## Vector Analysis in Computational Dialectometry



## Outline

- Vector Analysis: basics
- Idea: Vector Analysis in Computational Dialectometry
- Realisation
- Results
- Comparison: VA \& Informationtheory (Entropy)
- Future Work in Project Buldialect


## Basics

- Vector analysis is a subfield of geometry.
- Every array (e.g. vectors) has a starting point and an end point in a two- or more dimensional coordinate system. They determine the length and the direction of the vector.


## Basics

- The length of a vector:

$$
|\vec{v}|=\sqrt{\Delta x^{2}+\Delta y^{2}}
$$

- Angle $\alpha$ between two vectors:

$$
\cos (\alpha)=\frac{\vec{a} \cdot \vec{b}}{|\vec{a}| \cdot|\vec{b}|}
$$

## Vector Analysis in Computational Dialectometry



## The Idea

- Keep the focus on one interesting element (uni-, bi-, trigram, ...)
- Follow that element through the whole data-site
- Record the position-changes of that element
- Build a chain of vectors through the data
- Compare the position-changes from different datasites


## In Detail

- Following an element (here: A) through the data-site:


One element per word:
$x x x$ Ayyy
$x x x A y y y$
$x A x x y y y$

A missing element:
$x x x A y y y$
xxxxyyy
xAxxyyy

2 elements in one word:

$$
\begin{aligned}
& x x x \mathbf{A} y y y \\
& x x x x y y y \\
& x \mathbf{A x x} \mathbf{A y y}
\end{aligned}
$$

## Example, following the element "e":

"jA
"jAgne
be"li
"berAt
"beSe
brA"n_je
"brASno
*"br_=Ze
"beme
veZ"dA
"vece
"vet_Ser
"vet_SAr

## Analysis

Question: How to calculate site specific, individual values for every site?

## Answer(s):

- Using the angle between the single vectors to sum up the movement of the element
- Summing up the length of the single vectors to the length of the whole vector chain


## Question

- Ordering of the word lists?
- At the moment: alphabetic order
- Possible solution: using randomly ordered word lists


## Analysis

- Using the length of a vector chain takes into account the number of the element and position changes, while the angle between vectors would just count position changes

$$
\begin{aligned}
& \text { xxxAyyy } \\
& \text { a } \\
& \text { xxxAyyy } \quad|\vec{a}|<|\vec{b}| \\
& \text { xA } \\
& \text { xAxyyy }
\end{aligned}
$$

## Which element to follow?

- Examinations are possible in two directions:
- Single-word-all-sites, a so called SWAS-trace, is an examination of one word in all sites. For example, the word "red" in all sites
- Single-site-all-words, a SSAW-trace, examines all different words of a site, for example the complete list of words in site $x$

SSAW

|  | Aldomirovci | Asparuhovo | $\ldots$ | Zheravna |
| :--- | :---: | :---: | :---: | :---: |
| агне (lamb) | "jAgne | "Agni | $\ldots$ | ".. |
| аз (I) | "jA | "As | $\ldots$ | ".. |
| бели (white-plural) | "beli | "beli | $\ldots$ | ". |
| берат (pick up - 3rd plural) | "beru | bi"r7t | $\ldots$ | ... |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| ям (eat, 1st singular) | e"dem | "jAm | $\ldots$ | $\ldots$ |

SWAS

## Which element to follow?

- Using the SWAS direction for identifying the elements with the most position changes in the data set:

| X-Sampa code | Length of Vector Chain |
| :--- | :--- |
| e | 40015.1759910523 |
| stress | 35731.207131129 |
| 7 (close-mid back, unrounded) | 35653.6778159966 |
| A | 35432.7572223606 |
| i | 34438.756791175 |
| u | 34120.3965759371 |
| n | 33581.1330654058 |
| s | 33038.0473845845 |
| o | 32878.0780176776 |
| j (palatalized) | 32317.4612226377 |

## First results

- Uni-grams
- Analysis of vowels is more informative than consonants
- Clear distinction between the east and the west of Bulgaria


## Vector Analysis in Computational Dialectometry

## First results: East- west




Vertical Vectors


## Vector Analysis in Computational Dialectometry



## Comparison: Information Theory and Vector Analysis

Information Theory
Bigrams
Corpus based
Takes all elements into account
Ignores position of elements
Number of elements are measured

Vector Analysis
Focused Element
Word based
Uses just single elements
Tracks position of elements
Number of elements influences the VC

## Future work in Vector Analysis

- Using other structures than Uni-grams
- Use of randomly ordered word lists
- Combining the vector-based-approach with other approaches


## Future work in general

- Different clustering methods
- Classifiers instead of clustering
- More complex analysis in GIS

