

Exercise sheet 2

(Submit by email to dm@ling.osu.edu before class on Tuesday, January 20)

Provide Prolog definitions for the following relations. Thoroughly test it before handing it in!

1. `next_to_last/2`: a two place relation which takes a list as first argument and returns the next to last element of that list (if there is one) as second argument; i.e., `last(+List, -Next-to-Last-List-element)`

Example queries:

```
?- next_to_last([a,b,c,d],X). => X=c
?- next_to_last([a,b,c],X). => X=b
?- next_to_last([],X). => no
```

2. `wrap_with_f/2`: a two place relation which takes a list and returns the same list with the functor `f` wrapped around every element; i.e., `wrap_with_f(+List, -List-With-f-Wrapped-Elements)`

Example queries:

```
?- wrap_with_f([a,b,c,d],X). => [f(a),f(b),f(c),f(d)]
?- wrap_with_f([],X). => X=[]
```

3. `delete_b/2`: a two place relation which takes a list and deletes one occurrence of `b` (if there is one); i.e., `delete_b(+List, -List-with-one-b-less)`

Example queries:

```
?- delete_b([b,e,b,d],X). => X=[e,b,d]; X=[b,e,d]
?- delete_b([e,b,c,b,g,h],X). => X=[e,c,b,g,h]; X=[e,b,c,g,h]
?- delete_b([e,g,b],X). => X=[e,g]
?- delete_b([e,g,b,b],X). => X=[e,g,b]; X=[e,g,b]
?- delete_b([e,c],X). => no
```

Define the relation `delete_one_b` that removes only the first occurrence of a `b`.

```
?- delete_one_b([b,e,b,d],X). => X=[e,b,d]
?- delete_one_b([e,b,c,b,g,h],X). => X=[e,c,b,g,h]
?- delete_one_b([e,g,b],X). => X=[e,g]
?- delete_one_b([e,g,b,b],X). => X=[e,g,b]
?- delete_one_b([e,c],X). => no
```

4. `last_added_first/2`: a two place relation which takes a list and returns the same list with the last element of the input list added to the beginning of the result; i.e., `last_added_first(+List,-List-With-Last-Added-First)`

Example queries:

```
?- last_added_first([a,b,c,d],X). => [d,a,b,c,d]
?- last_added_first([a,b,c],X). => [c,a,b,c]
?- last_added_first([],X). => no
```

5. `in_list/2`: a two place relation which succeeds if the first list is a sublist (with sublist being reflexive) of the second; i.e., `in_list(+Sublist,+List)`

Example queries:

```
?- in_list([b,c],[a,b,c,d]). => yes
?- in_list([b,c],[b,c]). => yes
?- in_list([b,c],[a,b,b,c,d]). => yes
?- in_list([a,b],[a,b,c,d]). => yes
?- in_list([a,b,c],[a,b,c,d]). => yes
?- in_list([a],[a,b,c,d]). => yes
?- in_list([], [a,b,c,d]). => no
?- in_list([a,c],[a,b,c,d]). => no
?- in_list([b,d],[a,b,c,d]). => no
```

6. `mix/2`: a two place relation which takes a list as its first argument and returns as second argument each list that consists of all and only the elements of the input list in any order of occurrence; i.e., `mix(+List,-Mixed-list)`

Example queries:

```
?- mix([a,b,c],X). => X = [a,b,c] ; X = [b,a,c] ; X = [b,c,a] ; X = [a,c,b]
; X = [c,a,b] ; X = [c,b,a]
```

Hint: in defining `mix` it is useful to define an auxiliary relation `insert` which inserts a single element into an input list at any arbitrary position of the list and returns this newly constructed list.