 Finite-State Machines and Regular Languages Detmar Meurers: Intro to Computational Linguistics I OSU, LING 684.01, 8. January 2004 Determine the part-of-speech of words like the following, even if you can't find them in the dictionary: conurbation, cadence, disproportionality, lyricism, parlance Such tasks can be addressed using so-called finite-state machines. How can such machines be specified? When you call (614) 292-8833, you reach the fax machine. Find multiple adjacent occurrences of the same word in a text, as in I read the the book. Determine the language of the following utterance: French or Polish? 		More useful tasks involving language	
 Some useful tasks involving language Find all phone numbers in a text, e.g., occurrences such as When you call (614) 292-8833, you reach the fax machine. Find multiple adjacent occurrences of the same word in a text, as in I read the the book. Determine the language of the following utterance: French or Polish? 	Finite-State Machines and Regular Languages Detmar Meurers: Intro to Computational Linguistics I OSU, LING 684.01, 8. January 2004	 Look up the following words in a dictionary: <i>laughs, became, unidentifiable, Thatcherization</i> Determine the part-of-speech of words like the following, even if you can't find them in the dictionary: <i>conurbation, cadence, disproportionality, lyricism, parlance</i> ⇒ Such tasks can be addressed using so-called finite-state machines. ⇒ How can such machines be specified? 	
 Find all phone numbers in a text, e.g., occurrences such as <i>When you call (614) 292-8833, you reach the fax machine.</i> Find multiple adjacent occurrences of the same word in a text, as in <i>I read the the book.</i> Determine the language of the following utterance: French or Polish? A regular expression is a description of a set of strings, i.e., a language. A regular expression is a description of a set of strings, i.e., a language. A variety of unix tools (grep, sed), editors (emacs), and programming languages (perl, python) incorporate regular expressions. Just like any other formalism, regular expressions as such have no linguistic contents, but they can be used to refer to linguistic units. 	Some useful tasks involving language	3 Regular expressions	
Czy pasazer jadacy do Warszawy moze jechac przez Londyn?	 Find all phone numbers in a text, e.g., occurrences such as <i>When you call (614) 292-8833, you reach the fax machine.</i> Find multiple adjacent occurrences of the same word in a text, as in <i>I read the the book.</i> Determine the language of the following utterance: French or Polish? <i>Czy pasazer jadacy do Warszawy moze jechac przez Londyn?</i> 	 A regular expression is a description of a set of strings, i.e., a language. They can be used to search for occurrences of these strings A variety of unix tools (grep, sed), editors (emacs), and programming languages (perl, python) incorporate regular expressions. Just like any other formalism, regular expressions as such have no linguistic contents, but they can be used to refer to linguistic units. 	

The syntax of regular expressions (1)	The syntax of regular expressions (3)
<pre>Endpoint of the section of the</pre>	Operator precedence, from highest to lowest: parentheses () counters * + ? character sequences disjunction Note: The various unix tools and languages differ w.r.t. the exact syntax of the regular expressions they allow.
 The syntax of regular expressions (2) counters optionality: ? colou?r any number of occurrences: * (Kleene star) [0-9]* years at least one occurrence: + [0-9]+ dollars wildcard for any character: . beg.n for any character in between beg and n 	 Regular languages How can the class of regular languages which is specified by regular expressions be characterized? Let Σ be the set of all symbols of the language, the alphabet, then: {} is a regular language ∀a ∈ Σ: {a} is a regular language If L₁ and L₂ are regular languages, so are: the concatenation of L₁ and L₂: L₁ · L₂ = {xy x ∈ L₁, y ∈ L₂} the union of L₁ and L₂: L₁ · L₂ the union of L₁ and L₂: L₁ · L₂

Properties of regular languages

The regular languages are closed under (L_1 and L_2 regular languages):

- concatenation: $L_1 \cdot L_2$ set of strings with beginning in L_1 and continuation in L_2
- Kleene closure: L_1^* set of repeated concatenation of a string in L_1
- union: $L_1 \cup L_2$ set of strings in L_1 or in L_2
- complementation: $\Sigma^* L_1$ set of all possible strings that are not in L_1
- difference: $L_1 L_2$ set of strings which are in L_1 but not in L_2

Finite state machines

Finite state machines (or automata) (FSM, FSA) recognize or generate regular languages, exactly those specified by regular expressions.

Example:

- Regular expression: colou?r
- Finite state machine:



- intersection: L₁ ∩ L₂ set of strings in both L₁ and L₂
- reversal: L_1^R set of the reversal of all strings in L_1

Defining finite state automata

A finite state automaton is a quintuple (Q, Σ, E, S, F) with

- Q a finite set of states
- Σ a finite set of symbols, the alphabet
- $S \subseteq Q$ the set of start states
- $F \subseteq Q$ the set of final states
- *E* a set of edges $Q \times (\Sigma \cup \{\epsilon\}) \times Q$

The **transition function** *d* can be defined as

 $d(q,a) = \{q' \in Q | \exists (q,a,q') \in E\}$

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Language accepted by an FSA Example for a finite state transition network The extended set of edges $\hat{E} \subseteq Q \times \Sigma^* \times Q$ is the smallest set such that (S0) c b (S3 • $\forall (q, \sigma, q') \in E : (q, \sigma, q') \in \hat{E}$ • $\forall (q_0, \sigma_1, q_1), (q_1, \sigma_2, q_2) \in \hat{E} : (q_0, \sigma_1 \sigma_2, q_2) \in \hat{E}$ Regular expression specifying the language generated or accepted by the corresponding FSM: ab | cb+ The language L(A) of a finite state automaton A is defined as $L(A) = \{ w | q_s \in S, q_f \in F, (q_s, w, q_f) \in \hat{E} \}$ 13 15 Finite state transition networks (FSTN) Finite state transition tables Finite state transition networks are graphical descriptions of finite state Finite state transition tables are an alternative, textual way of describing machines: finite state machines: nodes represent the states • the rows represent the states • start states are marked with a short arrow start states are marked with a dot after their name • final states are indicated by a double circle final states with a colon • the columns represent the alphabet • arcs represent the transitions • the fields in the table encode the transitions 14 16

_		а	b	С	d
	S0.	S1		S2	
	S1		S3:		
	S2		S2,S3:		
	S3:				

Some properties of finite state machines

- Recognition problem can be solved in linear time (independent of the size of the automaton).
- There is an algorithm to transform each automaton into a unique equivalent automaton with the least number of states.



- A finite state automaton is deterministic iff it has
- no ϵ transitions and
- for each state and each symbol there is at most one applicable transition.

Every non-deterministic automaton can be transformed into a deterministic one:

- Define new states representing a disjunction of old states for each non-determinacy which arises.
- Define arcs for these states corresponding to each transition which is defined in the non-deterministic automaton for one of the disjuncts in the new state names.

Example: Determinization of FSA





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