

Problem: Inefficiency of recomputing subresults

Remembering subresults (Part I): Well-formed substring tables

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Two example sentences and their potential analysis:

- (1) He [gave [the young cat] [to Bill]].
- (2) He [gave [the young cat] [some milk]].

The corresponding grammar rules:

vp ---> [v_ditrans, np, pp_to].
vp ---> [v_ditrans, np, np].

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Solution: Memoization

- Store intermediate results:
 - a) completely analyzed constituents:
well-formed substring table or **(passive) chart**
 - b) partial and complete analyses:
(active) chart
- All intermediate results need to be stored for completeness.
- All possible solutions are explored in parallel.

CFG Parsing: The Cocke Younger Kasami Algorithm

- Grammar has to be in Chomsky Normal Form (CNF), only
 - RHS with a single terminal: $A \rightarrow a$
 - RHS with two non-terminals: $A \rightarrow BC$
 - no ϵ rules ($A \rightarrow \epsilon$)
- A representation of the string showing positions and word indices:

$\cdot_0 w_1 \cdot_1 w_2 \cdot_2 w_3 \cdot_3 w_4 \cdot_4 w_5 \cdot_5 w_6 \cdot_6$

For example: \cdot_0 the \cdot_1 young \cdot_2 boy \cdot_3 saw \cdot_4 the \cdot_5 dragon \cdot_6

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The well-formed substring table (= passive chart)

- The well-formed substring table, henceforth (passive) chart, for a string of length n is an $n \times n$ matrix.
- The field (i, j) of the chart encodes the set of all categories of constituents that start at position i and end at position j , i.e.
 $\text{chart}(i, j) = \{A \mid A \Rightarrow^* w_{i+1} \dots w_j\}$
- The matrix is triangular since no constituent ends before it starts.

Coverage Represented in the Chart

An input sentence with 6 words:

$\cdot_0 w_1 \cdot_1 w_2 \cdot_2 w_3 \cdot_3 w_4 \cdot_4 w_5 \cdot_5 w_6 \cdot_6$

Coverage represented in the chart:

		TO:					
		1	2	3	4	5	6
FROM:	0	0-1	0-2	0-3	0-4	0-5	0-6
	1		1-2	1-3	1-4	1-5	1-6
	2			2-3	2-4	2-5	2-6
	3				3-4	3-5	3-6
	4					4-5	4-6
	5						5-6

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Example for Coverage Represented in Chart

Example sentence:

\cdot_0 the \cdot_1 young \cdot_2 boy \cdot_3 saw \cdot_4 the \cdot_5 dragon \cdot_6

Coverage represented in chart:

	1	2	3	4	5	6
0	the	the young	the young boy	the young boy saw	the young boy saw the	the young boy saw the dragon
1		young	young boy	young boy saw	young boy saw the	young boy saw the dragon
2			boy	boy saw	boy saw the	boy saw the dragon
3				saw	saw the	saw the dragon
4					the	the dragon
5						dragon

An Example for a Filled-in Chart

Input sentence:

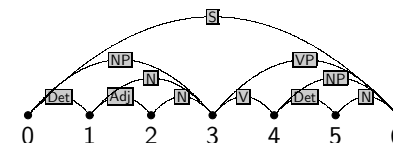
\cdot_0 the \cdot_1 young \cdot_2 boy \cdot_3 saw \cdot_4 the \cdot_5 dragon \cdot_6

Chart:

	1	2	3	4	5	6
0	{Det}	{}	{NP}	{}	{}	{S}
1		{Adj}	{N}	{}	{}	{}
2			{N}	{}	{}	{}
3				{V, N}	{}	{VP}
4					{Det}	{NP}
5						{N}

Grammar:

- $S \rightarrow NP VP$
- $VP \rightarrow Vt NP$
- $NP \rightarrow Det N$
- $N \rightarrow Adj N$
- $Vt \rightarrow \text{saw}$
- $Det \rightarrow \text{the}$
- $Det \rightarrow \text{a}$
- $N \rightarrow \text{dragon}$
- $N \rightarrow \text{boy}$
- $N \rightarrow \text{saw}$
- $Adj \rightarrow \text{young}$



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Filling in the Chart

- It is important to fill in the chart systematically.
- We build all constituents that end at a certain point before we build constituents that end at a later point.

	1	2	3	4	5	6
0	1	3	6	10	15	21
1		2	5	9	14	20
2			4	8	13	19
3				7	12	18
4					11	17
5						16

```

for j := 1 to length(string)
  lexical_chart_fill(j - 1, j)
  for i := j - 2 down to 0
    syntactic_chart_fill(i, j)
  
```

lexical_chart_fill(j-1,j)

- Idea: Lexical lookup. Fill the field $(j - 1, j)$ in the chart with the preterminal category dominating word j .
- Realized as:

$$chart(j - 1, j) := \{X \mid X \rightarrow \text{word}_j \in P\}$$

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syntactic_chart_fill(i,j)

- Idea: Perform all reduction step using syntactic rules such that the reduced symbol covers the string from i to j .

• Realized as: $chart(i, j) = \left\{ A \mid \begin{array}{l} A \rightarrow BC \in P, \\ i < k < j, \\ B \in chart(i, k), \\ C \in chart(k, j) \end{array} \right\}$

- Explicit loops over every possible value of k and every context free rule:

```

chart(i, j) := {}.
for k := i + 1 to j - 1
  for every A → BC ∈ P
    if B ∈ chart(i, k) and C ∈ chart(k, j) then
      chart(i, j) := chart(i, j) ∪ {A}.
  
```

The Complete CYK Algorithm

Input: start category S and input $string$

$n := \text{length}(string)$

for $j := 1$ to n

$chart(j - 1, j) := \{X \mid X \rightarrow \text{word}_j \in P\}$

for $i := j - 2$ down to 0

$chart(i, j) := \{\}$

for $k := i + 1$ to $j - 1$

for every $A \rightarrow BC \in P$

if $B \in chart(i, k)$ and $C \in chart(k, j)$ then
 $chart(i, j) := chart(i, j) \cup \{A\}$

Output: if $S \in chart(0, n)$ then accept else reject

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Dynamic knowledge bases in PROLOG

- Declaration of a dynamic predicate: `dynamic/1` declaration, e.g:
`:- dynamic chart/3.`
to store facts of the form `chart(From,To,Category)`:
- Add a fact to the database: `assert/1`, e.g.:
`assert(chart(1,3,np)).`
Special versions `asserta/1/assertz/1` ensure adding facts first/last.
- Removing a fact from the database: `retract/1`, e.g.:
`retract(chart(1,_,np)).`
To remove all matching facts from the database use `retractall/1`

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The CYK algorithm in PROLOG (parser/cky/cky.pl)

```
:- dynamic chart/3.           % chart(From,To,Category)
:- op(1100,xfx,'--->').     % Operator for grammar rules

% recognize(+WordList,?Startsymbol): top-level of CYK recognizer

recognize(String,Cat) :-
    retractall(chart(_,_,_)), % initialize chart
    length(String,N),         % determine length of string
    fill_chart(String,0,N),   % call parser to fill the chart
    chart(0,N,Cat).           % check whether parse successful
```

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```
% fill_chart(+WordList,+Current minus one,+Last)
% J-LOOP from 1 to n

fill_chart([],N,N).
fill_chart([W|Ws],JminOne,N) :-
    J is JminOne + 1,
    lexical_chart_fill(W,JminOne,J),
    %
    I is J - 2,
    syntactic_chart_fill(I,J),
    %
    fill_chart(Ws,J,N).
```

```
% lexical_chart_fill(+Word,+JminOne,+J)
% fill diagonal with preterminals

lexical_chart_fill(W,JminOne,J) :-
    (Cat ---> [W]),
    add_to_chart(JminOne,J,Cat),
    fail
; true.
```

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```

% syntactic_chart_fill(+I,+J)
% I-LOOP from J-2 downto 0

syntactic_chart_fill(-1,_) :- !.
syntactic_chart_fill(I,J) :-
    K is I+1,
    build_phrases_from_to(I,K,J),
    %
    IminOne is I-1,
    syntactic_chart_fill(IminOne,J).

```

```

% build_phrases_from_to(+I,+Current-K,+J)
% K-LOOP from I+1 to J-1

build_phrases_from_to(_,J,J) :- !.
build_phrases_from_to(I,K,J) :-
    chart(I,K,B),
    chart(K,J,C),
    (A ---> [B,C]),
    add_to_chart(I,J,A),
    fail
; KplusOne is K+1,
  build_phrases_from_to(I,KplusOne,J).

```

```

% add_to_chart(+Cat,+From,+To): add if not yet there
add_to_chart(From,To,Cat) :-
    chart(From,To,Cat),
    !.
add_to_chart(From,To,Cat) :-
    assertz(chart(From,To,Cat)).

```