

# Computational Linguistics II: Parsing

## *The CYK Parser*

Frank Richter & Jan-Philipp Söhn

[fr@sfs.uni-tuebingen.de](mailto:fr@sfs.uni-tuebingen.de), [jp.soehn@uni-tuebingen.de](mailto:jp.soehn@uni-tuebingen.de)

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- Consequence: inefficient behavior of the algorithms
- In order to avoid ‘reparsing’, a parser needs to remember partial results.

# Cocke-Younger-Kasami Parser – CYK

- The CYK parser uses chart for storing partial results.

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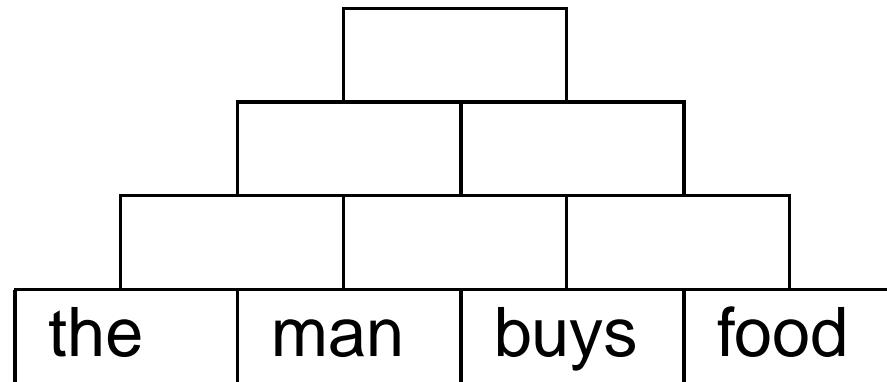
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# A few Definitions

## Definition 1

Two context free grammars  $G$  and  $G'$  are called *equivalent* iff  $L(G) = L(G')$ .

## Definition 2

A context free grammar  $G = \langle N, T, P, S \rangle$  is called  $\epsilon$ -free if it does not contain a production of the form  $A \rightarrow \epsilon$ , with the possible exception of  $S \rightarrow \epsilon$  in case  $\epsilon \in L(G)$ . In this case,  $S$  does not occur on the righthand side of a production rule in  $P$ .

## Definition 3

For each grammar  $G = \langle N, T, P, S \rangle$ , each  $p \in P$  of the form  $A \rightarrow B$  with  $A, B \in N$ , is called a *chain rule (unit rule)*.

# $\epsilon$ -free Type 2 Grammars (1)

## Lemma 1

There is an algorithm which for each context free grammar  $G = \langle N, T, P, S \rangle$  produces an equivalent  $\epsilon$ -free context free grammar  $G' = \langle N', T', P', S' \rangle$ .

Sketch of the procedure: Let

$$W_1 = \{A \in N \mid A \rightarrow \epsilon \in P\},$$

$$W_{i+1} = \{A \in N \mid A \rightarrow x \in P \text{ with } x \in W_i^*\} \cup W_i.$$

1.  $W_i \subseteq W_{i+1}$  ( $i \geq 1$ ),
2. If  $W_i = W_{i+1}$  then  $W_i = W_{i+m}$  for  $m \geq 0$ ,
3.  $W_n = W_{n+1}$ ,  $n = |N|$ ,
4.  $W_n = \{A \in N \mid A \rightarrow^* \epsilon\}$

# $\epsilon$ -free Type 2 Grammars (2)

Let

$N' = N \cup S'$ ,  $S'$  a new start symbol,

$T' = T$ ,

$P' = \{S' \rightarrow S\} \cup$

$\{A \rightarrow A_1 \dots A_k \mid k \geq 1, A_i \in N \cup T$

and there are  $x_1 \dots x_{k+1} \in W_n^*$  with

$A \rightarrow x_1 A_1 x_2 \dots A_k x_{k+1} \in P\} \cup P_\epsilon$ ,

with  $P_\epsilon = \{\}$  in case  $\epsilon \notin L(G)$ , else  $P_\epsilon = S' \rightarrow \epsilon$ .